

**University of Massachusetts Lowell**  
**Department of Electrical and Computer Engineering**  
**16.520 Computer Aided Engineering Analysis**  
**Problem set 1**

Note: all arguments must be passed by reference

1. Consider a  $N$  sided regular polygon inscribed in a circle of radius equal to  $1/2$ . The number of sides is given by  $N = 2^m$  where  $m = (2, 3, \dots)$ . When  $m = 2$  the perimeter of the square is equal to  $p_2 = 2^2 \sin(\pi/2^2) = 2\sqrt{2}$ . Note that as did Archimedes that as  $N$  approaches infinity  $p_\infty = \pi$ .

- a. Show that perimeter of a  $2^m$  sided polygon is equal to

$$p_m = 2^m \sin(\pi/2^m)$$

- b. Using the half angle formula can obtain the recursion

$$p_{m+1} = 2^{m+1/2} \sqrt{1 - \sqrt{1 - \left(\frac{p_m}{2^m}\right)^2}}$$

where  $p_2 = 2\sqrt{2}$ . Write a single precision program in Fortran or C to evaluate  $p_m$  as a function of  $m$  for  $m = 3, \dots, 14$ . Using gnuplot plot the error  $|p_m - \pi|$  versus  $m$  using a log y-axis and linear x-axis. Obtain a hardcopy of the result. Using this result what is the value of  $m$  that yields the minimum error.

2. Consider the product form expression for  $\sin(x)$

$$\text{sine}(x, NTERMS) = x \prod_{n=1}^{NTERMS} \left(1 - \frac{x^2}{p_n^2}\right)$$

where  $p_n = n\pi$  the zeroes of sine. As  $NTERMS$  approaches  $\infty$   $\text{sine}(x, NTERMS) \rightarrow \sin(x)$ .

- Write a single precision function routine in Fortran or C to evaluate the aforementioned expression. The function should be labeled  $\text{sine}(x, NTERMS)$  and return a real valued floating point result. The argument  $x$  is real and  $NTERMS$  is integer valued.
- Compare your result and the exact result graphically using  $NTERMS = 20$  for  $0 \leq x \leq 2\pi$  at  $x = k\Delta x$  where  $k = 0, NPTS - 1$ .  $NPTS = 100$ .
- How many terms are required to yield an absolute error,  $|\sin(x) - \text{sine}(x, NTERMS)| < 10^{-3}$ .

3. Download port3, unzip, untar, make library. Place the library libport3.a in your  $\sim$ /lib directory. Test library using given examples. Be sure to tell to compiler where the library is using the  $-L\sim$ /lib option and  $-lport3$  in gfortran.